



## Abstract

This paper focuses on the *multi-agent credit assignment* problem. We propose a novel multi-agent reinforcement learning algorithm called *meta imitation counterfactual regret advantage* (MICRA) and a three-phase framework for training, adaptation, and execution of MICRA. The key features are: (1) a *counterfactual regret advantage* is proposed to optimize the target agents' policy; (2) a meta-imitator is designed to infer the external agents' policies. Results show that MICRA outperforms state-of-the-art algorithms.

## Background: Stochastic Game

A stochastic game is defined as a 7-tuple  $\mathcal{G} = \langle S, N, A, T, R, O, \Omega \rangle$ , where:

- ▶  $S$  is a set of states.  $s^t$  is the state at time  $t$ ;
- ▶  $N = \{1, \dots, n\}$  is a set of  $n$  agents;
- ▶  $A = A_1 \times \dots \times A_n$  is a set of joint actions, where  $A_i$  is the agent  $i$ 's action set.  $\vec{a}^t = [a_1^t, \dots, a_n^t]$  is the joint action at time  $t$ ;
- ▶  $T : S \times A \times S \rightarrow [0, 1]$  is the transition probability function;
- ▶  $O = O_1 \times \dots \times O_n$  is a set of joint observations, where  $O_i$  is the agent  $i$ 's observation set. Joint observation at time  $t$  is  $\vec{o}^t = [o_1^t, \dots, o_n^t]$ ;
- ▶  $\Omega : S \times A \rightarrow O$  is the observation function;
- ▶  $R = \{R_1, \dots, R_n\}$  is the reward function set, where  $R_i : S \times A \rightarrow \mathbb{R}$  is the reward function for agent  $i$ .

## Background: Meta Learning

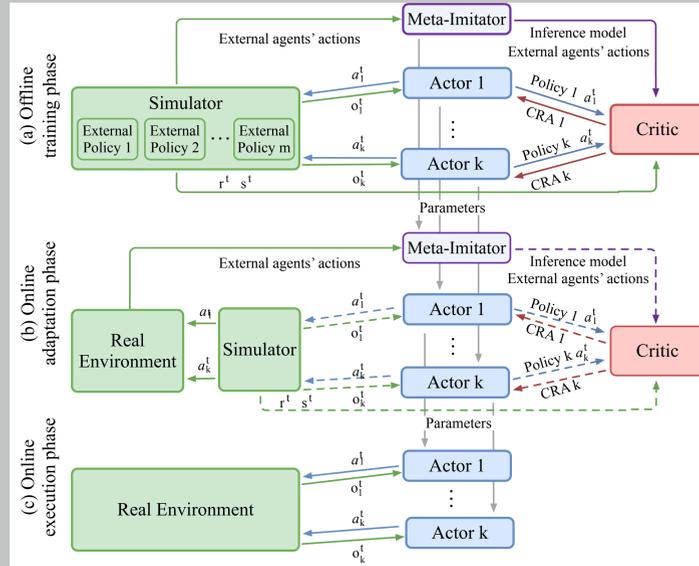
The objective of meta learning can be described as follows:

$$\min_{\theta} \mathbb{E}_{\mathcal{T}_i \sim \mathcal{T}} \left[ \sum_{t=1}^{H_i} \mathcal{L}_i(x^t, a^t) \right] \quad (1)$$

where  $x^{t+1} \sim P_i(\cdot | x^t, a^t)$ ,  $a^t \sim f(\cdot | x^0, x^1, \dots, x^t; \theta)$   
Meta-learning has been widely used in supervised learning, and single-agent reinforcement learning.

## Framework

The proposed three-phase framework integrates the CTDE (Lowe,17) paradigm with the meta-learning process (Finn,17).



## Algorithm: Counterfactual Regret Advantage

- (1) A centralized critic evaluates a *regret* value for an agent with the assumption that other agents follow the current policies; (2) Multiple actors independently update their individual policies minimizing the regret value.

*Immediate counterfactual regret advantage*:

$$\begin{aligned} \mathcal{A}_{T,i,\pi}^T(s, \vec{a}) &= v_{\pi^T | s \rightarrow a_i}(s) - v_{\pi^T}(s) \\ &= \sum_{\vec{a}_{-i}, \vec{a}_i} \pi_{T-i}^T(\vec{a}_{-i} | s) \pi_{\epsilon}^T(\vec{a}_i | s) Q(s, [a_i, \vec{a}_{-i}, \vec{a}_i]) \\ &\quad - \sum_{\vec{a}_{-i}, \vec{a}_i} \pi_{T-i}^T(\vec{a}_{-i} | s) \pi_{\epsilon}^T(\vec{a}_i | s) Q(s, [\vec{a}_{-i}, \vec{a}_i]) \end{aligned} \quad (2)$$

CRA based policy gradient:

$$g_{CRA,i} = \mathbb{E}_{s^t \sim D, \vec{a}^t \sim \pi} \left[ \sum_{t=0}^H \nabla_{\theta_i^t} \log(\pi_i(a_i^t | o_i^t; \theta_i^t)) \mathcal{A}_{i,\pi}^T(s^t, \vec{a}^t) \right] \quad (3)$$

## Algorithm: Meta Imitation Learning

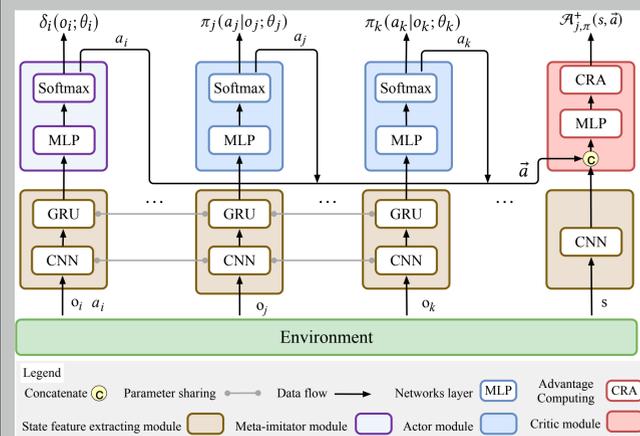
The objective of MI is:

$$\min_{\theta_i} \sum_{\mathcal{T}_i \sim p(\mathcal{T})} L_{\mathcal{H}_i}^{im}(\delta(\cdot; \theta'_i)) \quad (4)$$

$$\text{s.t. } \theta'_i = \theta_i - \alpha_{\text{adp}} \nabla_{\theta_i} L_{\mathcal{H}_i}^{im}(\delta(\cdot; \theta_i))$$

where  $p(\mathcal{T})$  is the distribution of all external agents' policies.  $\theta_i$  is the meta parameters which will be used as initial parameters in online adaptation phase.

## Algorithm: Network Structures



- ▶ *State feature extractor*, which extracts the high-level feature from the raw data.
- ▶ *Meta-imitator*, which monitors the external agents' observation-action pairs, and learns an inference model to predict their behaviors with meta-imitation learning. The module's output layer is softmax, which generates the probability of all available actions to the external agents.
- ▶ *Actor*, which trains the individual policy for each targeted agent using the CRA policy gradient.
- ▶ *Critic*, which trains a joint Q-function using temporal difference learning and computes CRA for instructing each actor to update its policy correctly.

## Evaluation

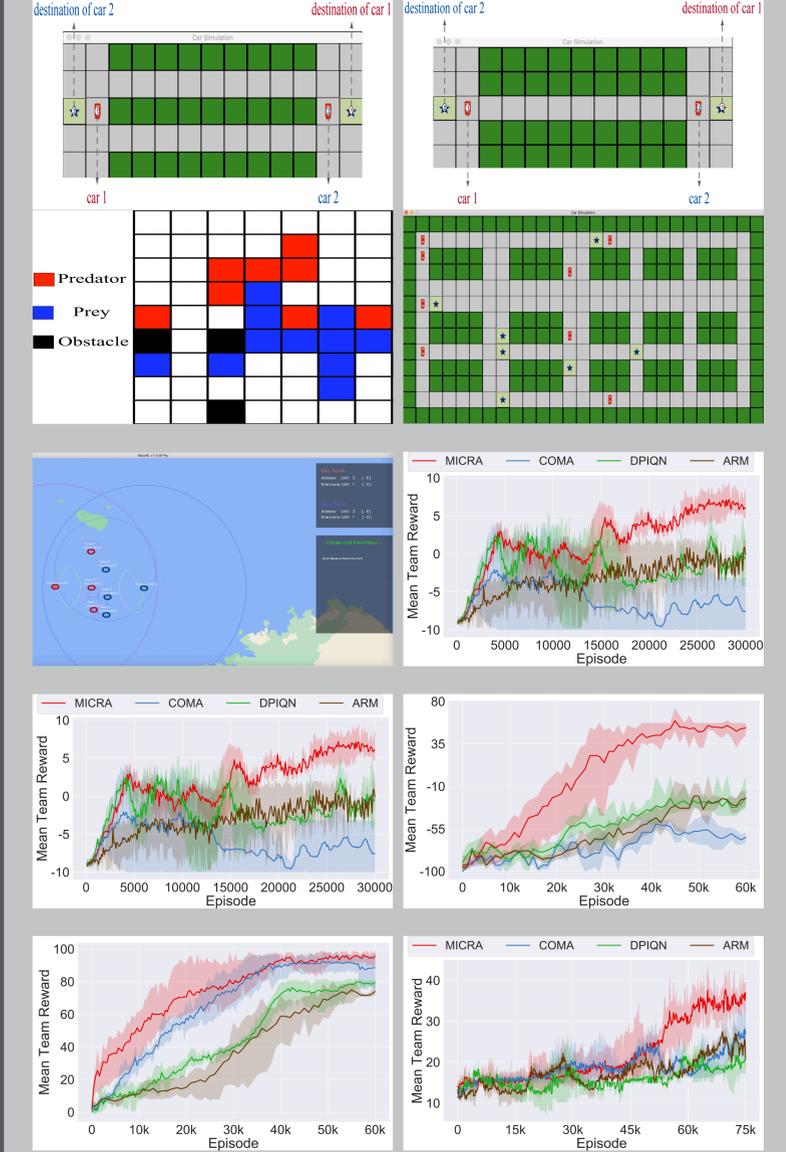


Figure: Offline training: the learning curves on different tasks (red line is ours).