

# Approximate Difference Rewards For Scalable Multiagent Reinforcement Learning

Arambam James Singh, Akshat Kumar and Hoong Chuin Lau, School of Computing & Information Systems, Singapore Management University {arambamjs.2016, akshatkumar, hclau}@smu.edu.sg

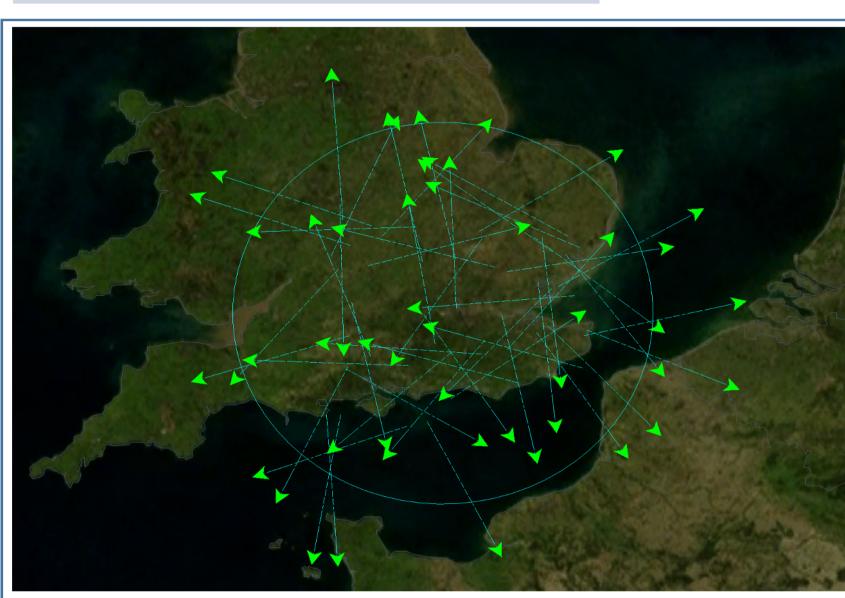


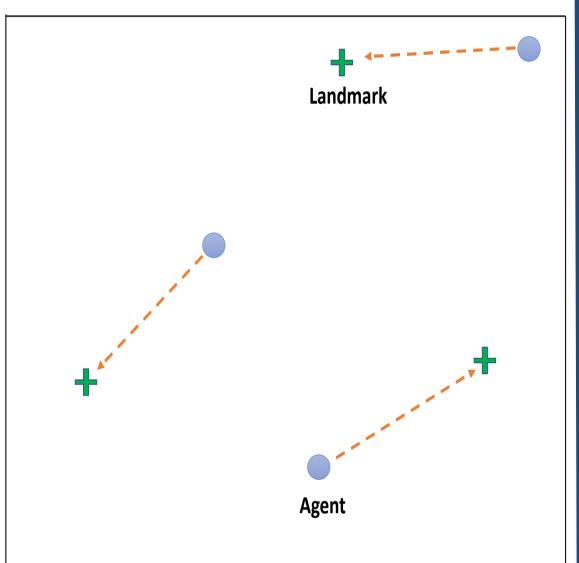
## Introduction

We address the problem of multiagent credit assignment in large scale multiagent system. Our main contributions are:

- An approach to learn a differentiable reward model by exploiting the collective nature of interactions among agents.
- A principled method to analytically compute shaped rewards from the reward model.
- A model-based RL approach that uses learned shaped rewards addressing credit assignment problem.

## Motivating Domain:





Air Traffic Control

Cooperative Navigation

## **Challenges:**

- Empirical reward signal is not effective in addressing multiagent credit assignment problem.
- The credit assignment problem becomes more challenging with large number of agents.
- Current proposed approaches either do not scale well for large agent settings or their credit assignment mechanism is not effective.

Our work address these challenges.

## Count Variables

## **State count variable:**

$$\mathbf{n}_t(s) = \sum_{m=1}^{M} \mathbb{I}[s_t^m = s; \boldsymbol{s}_t], \forall s \in S$$

## **State-action count variable:**

$$\mathbf{n}_t(s, a) = \sum_{m=1}^{N} \mathbb{I}[s_t^m = s, a_t^m = a; \boldsymbol{s}_t, \boldsymbol{a}_t], \forall s \in S$$

## System Reward Approximator

#### **❖System Reward:**

$$r\left(\mathbf{n}_{t}^{SA}\right) = \sum_{s \in S} \sum_{a \in A} \mathbf{n}_{t}(s, a) \cdot \tilde{r}(s, a, \mathbf{n}_{t}^{S})$$

### **Loss Function for Reward Approximator:**

$$\widetilde{\mathcal{L}}(\mathbf{w}) = M \sum_{\xi \in \mathcal{B}} \sum_{s \in S} \sum_{a \in A} \mathbf{n}_{\xi}(s, a) \cdot \left( \widetilde{r}(s, a, \mathbf{n}_{\xi}^{S}) - r_{\mathbf{w}}(s, a, \mathbf{n}_{\xi}^{S}) \right)^{2}$$

## Approximate Difference Reward

### **❖**Difference rewards (DRs):

$$D^{m}\left(s_{t}^{m}, a_{t}^{m}\right) = r\left(\boldsymbol{s}_{t}, \boldsymbol{a}_{t}\right) - r\left(\boldsymbol{s}_{t}^{-m} \cup d_{s}, \boldsymbol{a}_{t}^{-m} \cup d_{a}\right)$$

#### **Difference rewards with count variable:**

$$D^{m}(s_t^m, a_t^m) = r_{\mathbf{w}} \left( \mathbf{n}_t^{SA} \right) - r_{\mathbf{w}} \left( \mathbf{n}_t^{SA - (s_t^m, a_t^m) + (d_s, d_a)} \right)$$

#### **Difference rewards for state-action:**

$$D_t(s, a) = r\left(\mathbf{n}_t^{SA}\right) - r\left(\mathbf{n}_t^{SA} - \mathcal{I}^{sa} + \mathcal{I}^{d_s d_a}\right)$$

## **Approximate difference rewards:**

$$D_{t}(s,a) \approx \frac{1}{M} \cdot \left( \frac{\partial r_{\mathbf{w}} \left( \tilde{\mathbf{n}}_{t}^{SA} \right)}{\partial \tilde{\mathbf{n}}_{t}^{SA}(s,a)} - \frac{\partial r_{\mathbf{w}} \left( \tilde{\mathbf{n}}_{t}^{SA} \right)}{\partial \tilde{\mathbf{n}}_{t}^{SA}(d_{s},d_{a})} \right)$$

## Policy Gradient with DRs

## \* Return with difference rewards:

$$R_t^{dr} = \sum_{i=0}^{\infty} \gamma^i \left( \sum_{s \in S} \sum_{a \in A} \mathbf{n}_{t+i}(s, a) \cdot D_{t+i}(s, a) \right)$$

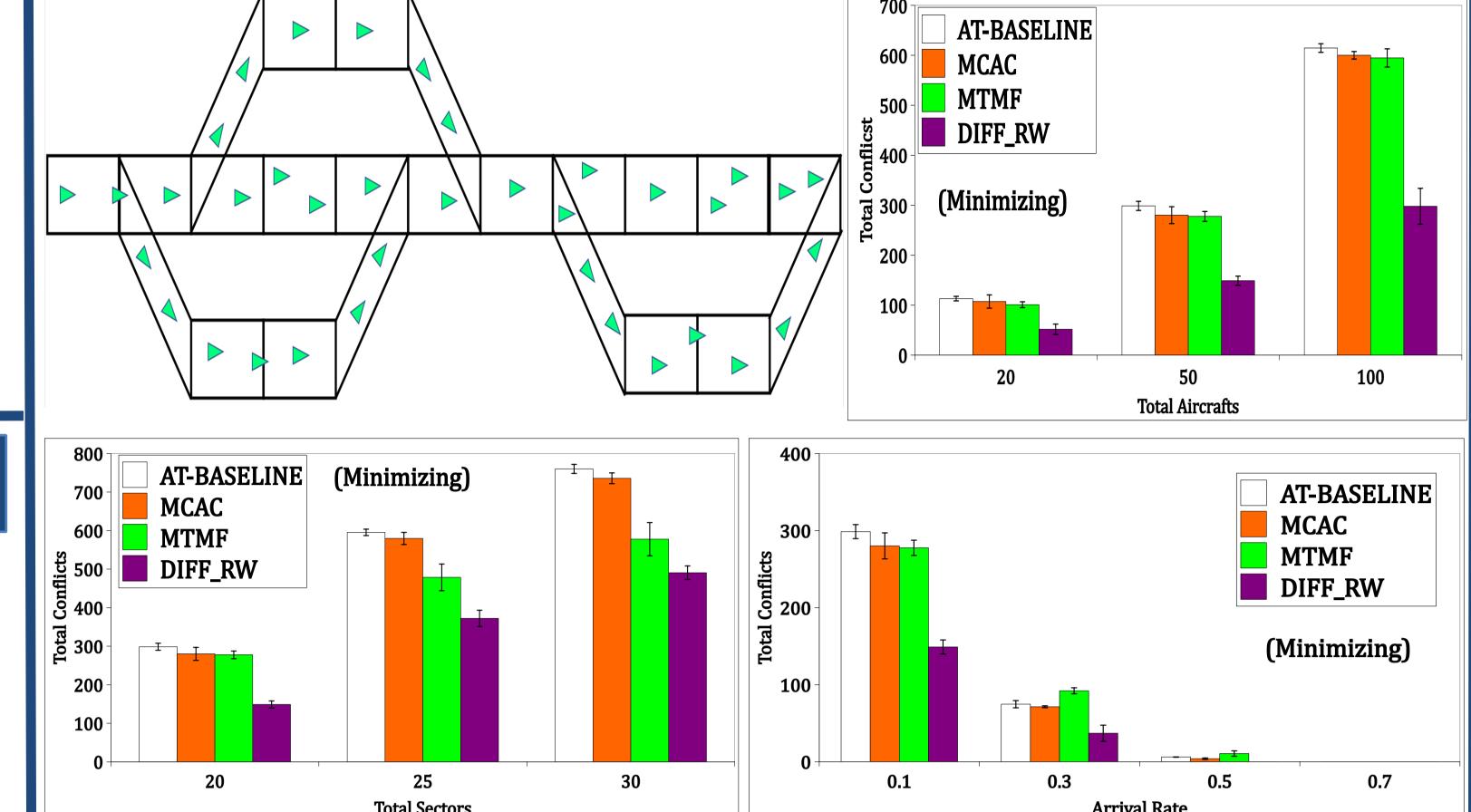
## Policy gradient:

$$\nabla_{\theta} J(\pi_{\theta}) = \mathbb{E}_{\boldsymbol{s}_{0:\infty}, \boldsymbol{a}_{0:\infty}} \left[ \sum_{t=0}^{\infty} \sum_{s \in S} \sum_{a \in A} n_{t}(s, a) \cdot \nabla_{\theta} \log \pi_{\theta}(a \mid s_{t}) \cdot R_{t}^{dr} \right]$$

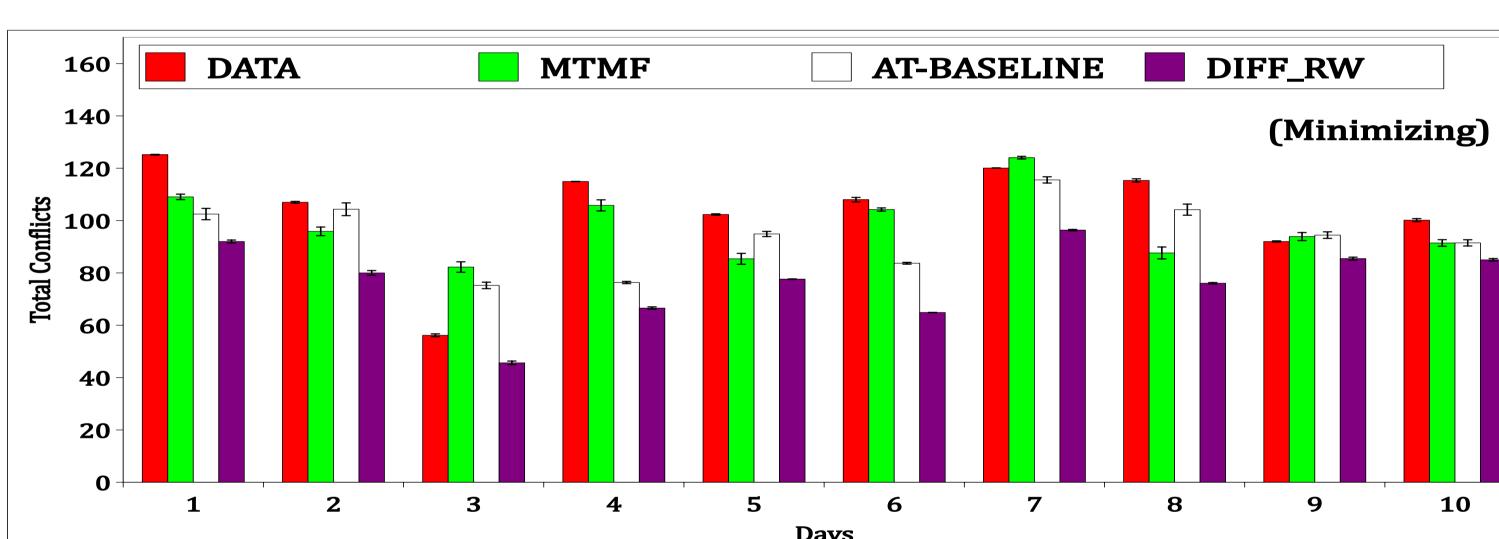
## Experiments

#### **Air Traffic Control:**

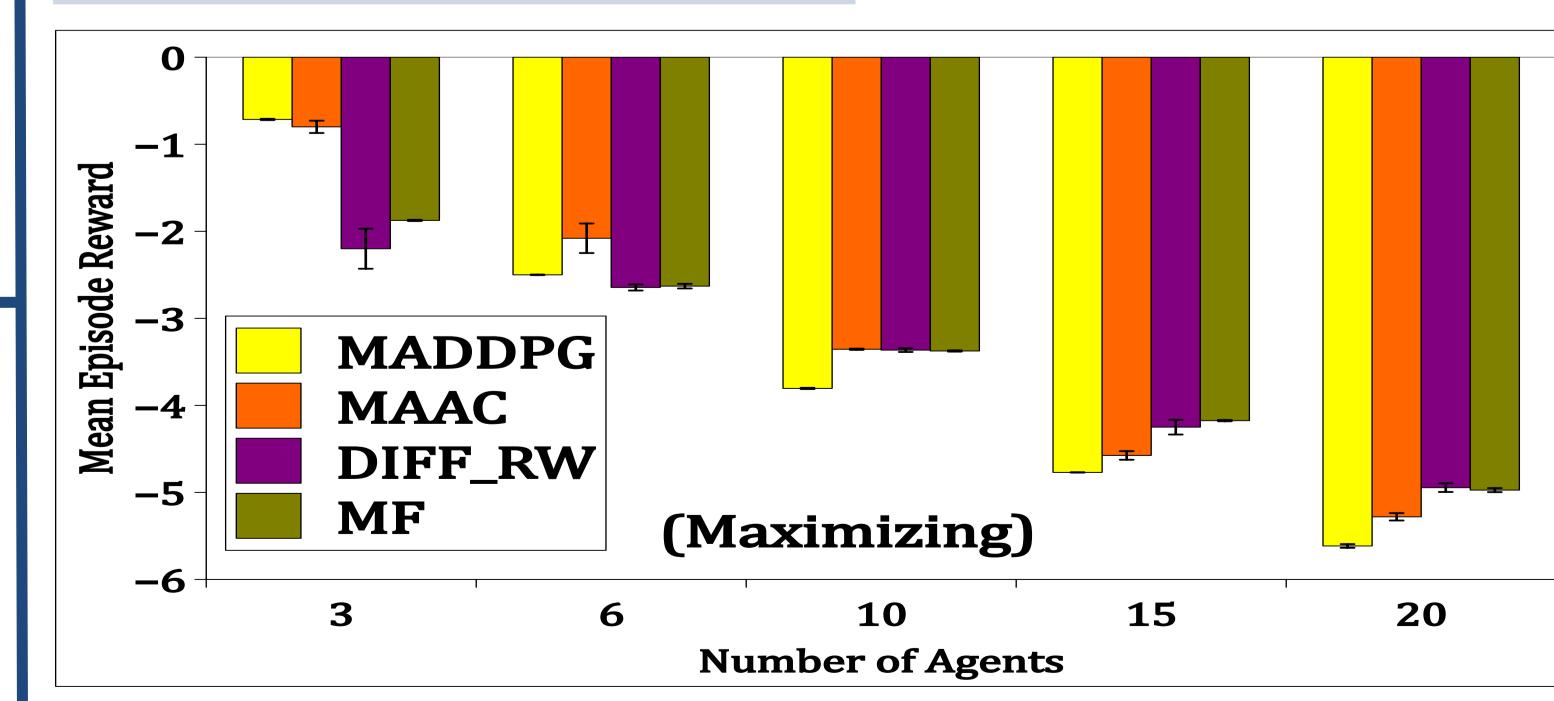




#### Real world dataset (1 month data):



## **Cooperative Navigation:**



## **Acknowledgments:**

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