# Argumentation-based reasoning in agents with varying degrees of trust

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# ABSTRACT

In any group of agents, trust plays an important role. The degree to which agents trust one another will inform what they believe, and, as a result the reasoning that they perform and the conclusions that they come to when that involves information from other agents. In this paper we consider a group of agents with varying degrees of trust of each other, and examine the combinations of trust with the argumentation-based reasoning that they can carry out. The question we seek to answer is "What is the relationship between the trust one agent has in another and the conclusions that it can draw using information from that agent?", and show that there are a range of answers depending upon the way that the agents deal with trust.

# **Categories and Subject Descriptors**

I.2.11 [**Artificial Intelligence**]: Distributed Artificial Intelligence— *Coherence & co-ordination; languages & structures; multiagent systems.* 

# **General Terms**

Language, theory.

# Keywords

Argumentation; Logic-based approaches and methods; Trust, reliability and reputation.

## 1. INTRODUCTION

Trust is an approach for measuring and managing the uncertainty about autonomous entities and the information they deal with. As a result trust can play an important role in any decentralized system. As computer systems have become increasingly distributed, and control in those systems has become more decentralized, trust has steadily become more important in computer science [5, 11].

Thus, for example, we see work on trust in peer-to-peer networks, including the EigenTrust algorithm [15] — a variant of PageRank [19] where downloads from a source play the role of outgoing hyperlinks and which is effective in excluding peers who

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want to disrupt the network — and the work in [1] that prevents peers manipulating their trust values to get preferential downloads. Zhong *et al.* [29] are concerned with slightly different issues in mobile ad-hoc networks, looking to prevent nodes from getting others to transmit their messages while refusing to transmit the messages of others, thus enforcing trustworthy behavior.

The internet, as the largest distributed system of all, is naturally a target of much of the research on trust. There have, for example, been studies on the development of trust in ecommerce [22], on mechanisms to determine which sources to trust when faced with multiple conflicting sources [28], and mechanisms for identifying which individuals to trust based on their past activity [2]. One interesting development is the idea of having individuals indemnify each other by placing some form of financial guarantee on transactions that others enter into [7, 8].

Trust is an especially important issue from the perspective of autonomous agents and multiagent systems [26]. The premise behind the multiagent systems field is that of developing software agents that will work in the interests of their "owners", carrying out their owners' wishes while interacting with other entities. In such interactions, agents will have to reason about the degree to which they should trust those other entities, whether they are trusting those entities to carry out some task, or whether they are trusting those entities to not misuse crucial information. As a result we find much work on trust in agent-based systems [24].

In such work it is common to assume that agents maintain a *trust network* of their acquaintances, which includes ratings of how much those acquaintances are trusted, and how much those acquaintances trust their acquaintances, and so on. An important line of inquiry in this context is what inference is reasonable in such networks, and the propagation of trust and provenance — both the transitivity of trust relations [23, 27] and more complex relationships like "co-citation" [12] have been studied, and in some cases empirically validated [12, 16, 28].

In this paper we look at the use of trust in other aspects of the reasoning that agents carry out. Argumentation [6] is a model of reasoning that seems well-suited to agent-based systems — it is robust against inconsistency, handles decision-making under uncertainty, and supports inter-agent communication. [20] suggests that argumentation is a suitable mechanism for reasoning about trust, and [18] shows how argumentation can be used to track trust in acquaintances. Here we investigate the combination of trust measures on agents and the use of argumentation for reasoning about trust and an existing system of argumentation.

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# 2. FORMAL MODEL

This paper deals with combining two formal models — a model of trust and a model of argumentation — and we introduce both here. Though there is no standard for either kind of model, we built as generic a model of both trust and argumentation as we could, drawing from well-established models in the literature. As a result we have a combined model that has a number of features unspecified — in later sections we will examine various instantiations.

#### 2.1 Trust

We are interested in a finite set of agents Ags and how these agents trust one another. Following the usual presentation (for example [16, 27, 23]), we start with a *trust relation*:

$$\tau \subseteq Ags \times Ags$$

which identifies which agents trust one another. If  $\tau(Ag_i, Ag_j)$ , where  $Ag_i, Ag_j \in Ags$ , then  $Ag_i$  trusts  $Ag_j$ . This is not a symmetric relation, so it is not necessarily the case that  $\tau(Ag_i, Ag_j) \Rightarrow$  $\tau(Ag_j, Ag_i)$ . It is natural to represent this trust relation as a directed graph, and we have:

DEFINITION 1. A trust network is a graph comprising, respectively, a set of nodes and a set of edges:

$$\mathcal{T} = \langle Ags, \{\tau\} \rangle$$

where Ags is a set of agents and  $\{\tau\}$  is the set of pairwise trust relations over Ags so that if  $\tau(Ag_i, Ag_j)$  is in  $\{\tau\}$  then  $\{Ag_i, Ag_j\}$ is a directed arc from  $Ag_i$  to  $Ag_j$  in T.

In this graph, the set of agents is the set of vertices, and the trust relations define the arcs. We are typically interested in *minimal* trust networks, which are connected — these thus capture the relationship between a set of agents all of whom, in one way or another are connected by a "web of trust". A directed path between agents in the trust network implies that one agent indirectly trusts another. For example if:

$$\langle Ag_1, Ag_2, \ldots Ag_n \rangle$$

is a path from agent  $Ag_1$  to  $Ag_n$ , then we have:

$$\tau(Ag_1, Ag_2), \tau(Ag_2, Ag_3), \ldots, \tau(Ag_{n-1}, Ag_n)$$

and the path gives us a means to compute the trust that  $Ag_1$  has in  $Ag_n$ . Below we will make use of the function  $length(\cdot)$  which returns the number of agents in a path:  $length(\langle Ag_1, Ag_2, \ldots Ag_n \rangle)$  is n.

The usual assumption in the literature is that we can place some measure on the trust that one agent has in another, so we have:

$$tr: Ags \times Ags \mapsto \Re$$

where tr gives a suitable trust value. In this paper, we take this value to be between 0, indicating no trust, and 1, indicating the greatest possible degree of trust. We assume that tr and  $\tau$  are mutually consistent, so that:

$$tr(Ag_i, Ag_j) \neq 0 \quad \Leftrightarrow \quad (Ag_i, Ag_j) \in \tau$$
$$tr(Ag_i, Ag_j) = 0 \quad \Leftrightarrow \quad (Ag_i, Ag_j) \notin \tau$$

Now, this just deals with the direct trust relations encoded in  $\tau$ . It is usual in work on trust to consider performing inference about trust by assuming that trust relations are transitive. This is easily captured in the notion of a trust network:

DEFINITION 2. If, in the trust network  $\mathcal{T}$ ,  $Ag_i$  is connected to  $Ag_j$  by a directed path  $\langle Ag_i, Ag_{i+1}, \ldots Ag_j \rangle$  then  $Ag_i$  trusts  $Ag_j$  according to  $\mathcal{T}$ 

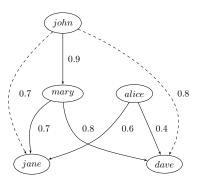


Figure 1: Example trust graph

The notion of trust embodied here is exactly Jøsang's "indirect trust" or "derived trust" [14] and the process of inference is what [12] calls "direct propagation". If we have a function tr, then we can compute:

$$tr(Ag_i, Ag_j) = tr(Ag_i, Ag_{i+1}) \otimes^{tr} tr(Ag_{i+1}, Ag_{i+2}) \otimes^{tr} \dots \otimes^{tr} tr(Ag_{j-1}, Ag_j)$$
(1)

for some operation  $\otimes^{tr}$ . Here we follow [27] in using the symbol  $\otimes$ , to stand for this generic operation<sup>1</sup>. Sometimes it is the case that there are two or more paths through the trust network between  $Ag_i$  and  $Ag_j$  indicating that  $Ag_i$  has several opinions about the trustworthiness of  $Ag_j$ . If these two paths are

 $\langle Ag_i, Ag'_{i+1}, \dots Ag_j \rangle$  and  $\langle Ag_i, Ag''_{i+1}, \dots Ag_j \rangle$ 

then the overall degree of trust that  $Ag_i$  has in  $Ag_j$  is:

$$tr(Ag_i, Ag_j) = tr(Ag_i, Ag_j)' \oplus^{tr} tr(Ag_i, Ag_j)''$$
(2)

Again we use the standard notation  $\oplus$  for a function that combines trust measures along two paths [27]. Clearly we can extend this to handle the combination of more than two paths.

Now, given this kind of propagation, we can define an order over the set of agents based on trust values. Since the trust measure we are using is relative to one agent,  $Ag_i$ , the order is necessarily relative that agent also. We have:

DEFINITION 3. For an agent  $Ag_i$ , a trust network  $\mathcal{T}$  and a trust measure tr, we can define an order over agents  $\succeq_i^{tr}$  such that  $Ag_j \succeq_i^{tr} Ag_k$  iff  $tr(Ag_i, Ag_j) \ge tr(Ag_i, Ag_k)$ . If this is the case, we say that  $Ag_i$  considers  $Ag_j$  at least as trustworthy as  $Ag_k$ .

We further define  $=_{i}^{tr}$  and  $\succ_{1}^{tr}$  in the usual way.  $Ag_{j} =_{i}^{tr} Ag_{k}$  iff  $Ag_{j} \succeq_{i}^{tr} Ag_{k}$  and  $Ag_{k} \succeq_{i}^{tr} Ag_{j}$ .  $Ag_{j} \succ_{i}^{tr} Ag_{k}$  iff  $Ag_{j} \succeq_{i}^{tr} Ag_{k}$  and  $Ag_{k} \succeq_{i}^{tr} Ag_{j}$ . In addition we extend all these relations to operate over a set of agents:  $Ags \succeq_{i}^{tr} Ags'$  iff  $Ag_{i}$  considers every  $Ag \in Ags$  at least as trustworthy as every  $Ag' \in Ags'$ .

As an example of a trust graph, consider Figure 1 (a) which shows the trust relationship between John, Mary, Alice, Jane and Dave. This is adapted from the example in [16] normalizing the values to lie between 0 and 1. The solid lines are direct trust relationships, the dotted lines are indirect links derived from the direct links. Thus John trusts Jane and Dave because he trusts Mary and Mary trusts Jane and Dave. However, John does not, even indirectly, trust Alice.

<sup>&</sup>lt;sup>1</sup>[12, 16, 23, 27], among others, provide different possible instantiations of this operation some of which we investigate below.

# 2.2 Argumentation

From the many formal argumentation systems in the literature, we take as our starting point the system from [21]. An agent  $Ag_i \in Ags$  maintains a knowledge base,  $\Sigma_i$ , containing a possibly inconsistent set of formulae of a propositional language  $\mathcal{L}$ . Agent *i* also maintains the set of its past utterances, called the "commitment store",  $CS_i$ . We refer to this as an agent's "public knowledge", since it contains information that is shared with other agents. In contrast, the contents of  $\Sigma_i$  are "private" to  $Ag_i$ .

Note that in the description that follows, we assume that  $\vdash$  is the classical inference relation, that  $\equiv$  stands for logical equivalence, and we use  $\Delta$  to denote all the information available to an agent. Thus in an interaction between two agents  $Ag_i$  and  $Ag_j$ ,  $\Delta_i = \Sigma_i \cup CS_i \cup CS_j$ , so the commitment store  $CS_i$  can be loosely thought of as a subset of  $\Delta_i$  consisting of the assertions that have been made public by  $Ag_i$ . In some dialogue games, such as those in [21] anything in  $CS_i$  is either in  $\Sigma_i$  or can be derived from it. In other dialogue games, such as those in [4],  $CS_i$  may contain things that cannot be derived from  $\Sigma_i$ .

DEFINITION 4. An argument A is a pair (S, p) where p is a formula of  $\mathcal{L}$  and S a subset of  $\Delta$  such that: (i) S is consistent; (ii)  $S \vdash p$ ; and (iii) S is minimal, so no proper subset of S satisfying both (i) and (ii) exists.

S is called the support of A, written S = Support(A) and p is the conclusion of A, written p = Conclusion(A). Thus we talk of p being supported by the argument (S, p).

In general, since  $\Delta$  may be inconsistent, arguments in  $\mathcal{A}(\Delta)$ , the set of all arguments which can be made from  $\Delta$ , may conflict, and we make this idea precise with the notion of *undercutting*:

DEFINITION 5. Let  $A_1$  and  $A_2$  be arguments in  $\mathcal{A}(\Delta)$ .  $A_1$ undercuts  $A_2$  iff there is some  $\neg p \in Support(A_2)$  such that  $p \equiv Conclusion(A_1)$ .

In other words, an argument is undercut if and only if there is another argument which has as its conclusion the negation of an element of the support for the first argument.

It will be typical for an agent  $Ag_i$  to have different degrees of belief  $bel_i(\cdot)$  for the formulae in  $\Delta_i$ , and in this paper we will assume that these belief values (like those in the much of the uncertainty handling literature) are between 0 and 1. Then, if there is some argument A = (S, p) and  $A \in \mathcal{A}(\Delta_i)$  we can compute the belief in an argument from the belief in the formulae in the support of the argument:

$$bel_i(A) = bel_i(s_1) \otimes^{bel} bel(s_2) \otimes^{bel} \dots \otimes^{bel} bel(s_n)$$
 (3)

where  $S = \{s_1, \ldots, s_n\}$ . Where we need to establish the belief in the conclusion p of A we will set  $bel_i(p)$  to be  $bel_i(A)$ . From these values we can then establish an order over arguments.

DEFINITION 6. For an agent  $Ag_i$  and a set of belief values for arguments  $bel_i(\cdot)$ , we can define an order over arguments  $\succeq_i^{bel}$ such that  $A_1 \succeq_i^{bel} A_2$  iff  $bel_i(A_1) \ge bel_i(A_2)$ . If this is the case, we say that  $Ag_i$  believes  $A_1$  at least as much as  $A_2$ .

In addition we say that  $A_1 =_i^{bel} A_2$  iff  $A_1 \succeq_i^{bel} A_2$  and  $A_2 \succeq_i^{bel} A_1$  and  $A_1 \succ_i^{bel} A_2$  iff  $A_1 \succeq_i^{bel} A_2$  and  $A_2 \succeq_i^{bel} A_1$ . As with the notion of belief on which they are grounded, we will use these relations between the conclusions of arguments when they hold for the arguments themselves.

We can now define the argumentation system we will use:

DEFINITION 7. An argumentation system is a triple:

$$\langle \mathcal{A}(\Delta_i), Undercut, \succ_i^{arg} \rangle$$

where  $\mathcal{A}(\Delta)$  is as defined as above,  $\succ_i^{arg}$  is a preference order over arguments, and Undercut is a binary relation collecting all pairs of arguments  $A_1$  and  $A_2$  such that  $A_1$  undercuts  $A_2$ .

Note that for now we don't define exactly where  $\succ_i^{arg}$  comes from — later we discuss how it can be established from  $\succ_i^{bel}$ . We say that  $A_1$  is *stronger than*  $A_2$  iff  $A_1 \succ_i^{arg} A_2$ .

The preference order makes it possible to distinguish different types of relations between arguments:

DEFINITION 8. Let  $A_1$ ,  $A_2$  be two arguments of  $\mathcal{A}(\Delta)$ .

- If  $A_2$  undercuts  $A_1$  then  $A_1$  defends itself against  $A_2$  iff  $A_1 \succ_i^{arg} A_2$ . Otherwise,  $A_1$  does not defend itself.
- A set of arguments A defends A<sub>1</sub> iff for every A<sub>2</sub> that undercuts A<sub>1</sub>, where A<sub>1</sub> does not defend itself against A<sub>2</sub>, then there is some A<sub>3</sub> ∈ A such that A<sub>3</sub> undercuts A<sub>2</sub> and A<sub>2</sub> does not defend itself against A<sub>3</sub>.

If  $A_1$  is undercut by  $A_2$  and either does not defend itself, or is not defended by another set of arguments, we say that  $A_1$  is *successfully undercut* and  $A_2$  is a successful undercutter. We write  $\mathcal{A}_{Undercut,\succ_i^{arg}}$  to denote the set of all arguments that are not successfully undercut (which includes those that are not undercut at all). The set  $\underline{\mathcal{A}}(\Delta)$  of acceptable arguments of the argumentation system  $\langle \mathcal{A}(\Delta), Undercut, \succ_i^{arg} \rangle$  is [3] the least fixpoint of a function  $\mathcal{F}$ :

$$\mathcal{A} \subseteq \mathcal{A}(\Delta)$$
  
 
$$\mathcal{F}(\mathcal{A}) = \{ (S, p) \in \mathcal{A}(\Delta) \mid (S, p) \text{ is defended by } \mathcal{A} \}$$

DEFINITION 9. The set of acceptable arguments for an argumentation system  $\langle \mathcal{A}(\Delta), Undercut, \succ_i^{arg} \rangle$  is recursively defined as:

$$\underline{\mathcal{A}}(\Delta) = \bigcup \mathcal{F}_{i \ge 0}(\emptyset)$$
$$= A_{Undercut, \succ_{i}^{arg}} \cup \left[\bigcup \mathcal{F}_{i \ge 1}(A_{Undercut, \succ_{i}^{arg}})\right]$$

An argument is acceptable if it is a member of the acceptable set, and a formula is acceptable if it is the conclusion of an acceptable argument.

An acceptable argument is one which is, in some sense, proven since all the arguments which might undermine it are themselves undermined. If there is an acceptable argument for a formula p, then the *status* of p is *accepted*, while if there is not an acceptable argument for p, the status of p is *not accepted*.

## 3. ARGUMENTATION AND TRUST

In this paper we are concerned with the following question. If an agent makes use of information that it gets from an acquaintance, how should the degree of trust the agent has in its acquaintance inform the way it uses the information? In particular, if an agent constructs arguments using this information, what, in general terms, is it reasonable for the agent to conclude? For example, we might want to specify that if an agent is given information that it doesn't trust very highly, then it should not allow conclusions derived from this information to over-rule conclusions derived from information provided by more trustworthy sources. However it is not immediately clear how to capture principles like this in formal models we introduced above.

#### 3.1 Combining trust and argumentation

To use our models of trust and argumentation to analyze this question, we first need to consider how to combine them. We opt for a very simple approach, adding a trust network to our existing definition of an argumentation system, so that a *trust argumentation system* is:

$$\langle Ags, \mathcal{A}(\Delta_i), Undercut, \succ_i^{arg}, \mathcal{T} \rangle$$

A trust argumentation system, then is specific to a given agent,  $Ag_i$ in the system above, and explicitly includes a set of agents Agsthat corresponds to the trust network T, and which are the agents whose commitment stores are combined with  $\Sigma_i$  to make up  $\Delta_i$ .

The argumentation system from the previous section allows  $Ag_i$  to construct arguments from:

$$\Delta_i = \Sigma_i \cup \{\bigcup_{j=1\dots n} CS_j\}$$

and now, thanks to the trust network,  $Ag_i$  can assign a trust value to each of the other agents<sup>2</sup> and hence to their commitment store. In addition, the argumentation model assumes that every formulae in  $\Delta_i$  can be assigned a belief value, and that there is a preference order  $\succ_i^{arg}$  over arguments that identifies the relative strength of arguments.

This model, as introduced, is deliberately vague about a number of issues, allowing us to define a whole family of trust argumentation systems, each of which includes a particular instantiation of the elements we have not specified. First, we need to know what functions to use for  $\otimes^{tr}$  and  $\oplus^{tr}$  in order to propagate trust values through the trust network in (1) and (2). Second we need to know how to use the trust value  $tr(Ag_i, Ag_j)$  that  $Ag_i$  puts on  $Ag_j$  to determine the belief that *i* places in information from  $CS_j$ . We can express that as a function  $ttb(\cdot)$  such that for some  $p \in CS_j$ 

$$bel_i(p) = ttb(tr(Ag_i, Ag_j)) \tag{4}$$

Third, we need to specify how the belief values  $bel_i(\cdot)$  are combined using (3) to establish the belief in an argument from the belief in individual formulae and hence the order  $\succ_i^{bel}$ . Fourth, we need to know how the preference order  $\succ_i^{arg}$ , which is used to determine acceptability, is established from  $\succ_i^{bel}$ .

The main aim of this paper is to explore some of these instantiations — different instantiations will give us different behaviors, and we will use the behaviors to evaluate the instantiations. Before we select instantiations we identify a number of desiderata which we want the instantiated trust argumentation system to adhere to.

#### **3.2 Desirable properties**

The properties we use are extracted from the literature, and our aim is to identify which make sense when used in combination with argumentation. Golbeck *et al.* [10] suggests that trust should follow the standard rules on network capacity, so that along any given path the maximum amount of trust between a source and a sink will be no larger than the smallest capacity along the path. In terms of propagating trust through a trust graph, this can be interpreted as saying that the trust that some agent  $Ag_i$  has in  $Ag_j$  is no greater than the minimum trust value along the path between them:

**PROPERTY** 1. If  $Ag_i$  is connected to  $Ag_{i+n}$  by a directed path  $\langle Ag_i, Ag_{i+1}, \ldots, Ag_{i+n} \rangle$  in a trust network where arcs are labelled with values  $tr(\cdot)$ , then:

$$tr(Ag_i, Ag_{i+n}) \le min_{j=0,\dots,n-1} tr(Ag_{i+j}, Ag_{i+j+1})$$

[10] also suggest that the length of the path between two agents is relevant in assessing the trust between the agents, and [13] suggests that "the weakening of trust through long transitive paths should result in a reduced confidence level". We will consider two different ways to interpret this. One says that a longer path will never lead to a stronger trust relation than a shorter path:

**PROPERTY** 2. If  $Ag_i$  is connected to  $Ag_j$  and  $Ag_k$  by two directed paths in a trust network, then  $tr(Ag_i, Ag_j) \leq tr(Ag_i, Ag_k)$  iff  $length(Ag_i, Ag_j) \geq length(Ag_i, Ag_k)$ .

The other interpretation says that trust values are monotonically non-increasing over paths:

**PROPERTY** 3. Given the directed path  $\langle Ag_i, \dots Ag_j, \dots Ag_k \rangle$ then  $tr(Ag_i, Ag_k) \leq (Ag_i, Ag_j)$ 

The above properties relate to  $\otimes^{tr}$ . There are also properties relating to  $\oplus^{tr}$ . The first comes from [13] which suggests that "combination of parallel trust paths should result in an increased confidence level". In other words:

**PROPERTY** 4. If  $Ag_i$  and  $Ag_j$  are linked by two paths in the trust network  $\mathcal{T}$ , and the trust computed along these paths are  $tr(Ag_i, Ag_j)'$  and  $tr(Ag_i, Ag_j)''$ , then the overall trust of  $Ag_i$  in  $Ag_j$ ,

$$tr(Ag_i, Ag_j) \ge max\left(tr(Ag_i, Ag_j)', tr(Ag_i, Ag_j)''\right)$$

The authors like to think of this as encoding the idea that having two letters of recommendation for a potential PhD student that say the student is excellent is no worse than having one. However, there is another desideratum that we might enforce here. If we have a potential PhD student with a multitude of recommendation letters that suggest they are a mediocre student, does this make them more highly recommended than a student with just a couple of letters suggesting that they are very good? The authors feel not, and so we also consider the property that combining two parallel trust paths does not cause the overall trust value to exceed the value defined by either path (which is one way to stop the many poor recommendations outweighing a few good ones for a different student).

PROPERTY 5. If  $Ag_i$  and  $Ag_j$  are linked by two paths in the trust network T, and the trust computed along these paths are  $tr(Ag_i, Ag_j)'$  and  $tr(Ag_i, Ag_j)''$ , then the overall trust of  $Ag_i$  in  $Ag_j$ ,

$$tr(Ag_i, Ag_j) \leq max\left(tr(Ag_i, Ag_j)', tr(Ag_i, Ag_j)''\right)$$

In different situations, either of these properties may be appropriate.

We can extend several of these ideas to deal with beliefs and their role in argumentation, in essence placing constraints on the the operation  $\bigotimes^{bel}$ . Thinking of an argument as a chain of inferences that make use of formulae from  $\Delta_i$  then an extension of Property 1 is that the conclusion of an argument should be believed no more than the minimum of the degrees of belief of all of the steps in the argument. This gives us:

**PROPERTY 6.** If  $Ag_i$  has an argument (S, p), and the support  $S = \{s_i, \ldots, s_m\}$ , then:

$$bel_i(p) \le min_{j=1,\dots,m}bel_i(s_j)$$

We can also extend Properties 2 and 3 to argumentation. This extension suggests that an argument that requires a larger support (and so in some sense is "longer") than another is less believable, and there are two obvious ways that we might capture this:

 $<sup>^{2}</sup>$ If there is no directed path between the two agents, then the value is 0.

PROPERTY 7. If  $Ag_i$  has two arguments (S, p) and (S', p'), then  $bel_i(p) \leq bel_i(p')$  iff  $|S| \geq |S'|$ .

which is analogous to P2 in saying that larger support never means a greater degree of belief, and:

**PROPERTY 8.** If  $Ag_i$  has two arguments (S, p) and (S', p'), then  $bel_i(p) \leq bel_i(p')$  if  $S \supseteq S'$ .

which is analogous to P3 in saying that adding additional formulae to a support cannot increase belief and is essentially Loui's [17] "directness" defeater.

The final property that we will consider here deals with the behavior of the combined trust and argumentation system, capturing one reading of the principle we outlined at the start of this section — the strength of an agent's arguments should reflect the trustworthiness of the agents from whom the support of those arguments was obtained. To capture this idea we need first to define:

DEFINITION 10. Given a set of agents  $Ags = \{Ag_1, \dots, Ag_n\}$ where each  $Ag_j$  has a commitment store  $CS_j$ , then a set of formulae S corresponds to the set of agents Ags' iff

$$Ags' = \{Ag_j | s \in S \text{ and } s \in CS_j\}$$

so that a set of formulae corresponds to the set of agents from whose commitment stores the formulae are drawn. Then we have:

**PROPERTY 9.** If  $Ag_i$  has two arguments (S, p) and (S', p'), where the supports have corresponding sets of agents Ag and Ag' then (S, p) is stronger than (S', p') only if  $Ag_i$  considers Ag to be more trustworthy than Ag'.

If this property is obeyed, then arguments grounded in information from less trustworthy sources will not be able to defeat arguments whose grounds are drawn from more trustworthy sources. In turn this means that:

**PROPOSITION 1.** In a trust argumentation system:

$$\langle Ags, \mathcal{A}(\Delta_i), Undercut, \succ_i^{arg}, \mathcal{T} \rangle$$

If an argument (S, p), with corresponding set of agents Ag, is acceptable, then, given Property 9, a new argument (S', p') with corresponding set of agents Ag' if  $Ag_i$  cannot make (S, p) not acceptable if  $Ag_i$  considers Ag' to be less trustworthy than Ag.

**PROOF.** If (S, p) is acceptable, then it is not successfully undercut, and so either (i) it is stronger than all its attackers, or (ii) it is defended by arguments that are stronger than those attackers that are stronger than it. Now consider that  $Ag_i$  learns enough information to create (S', p') which undercuts (S, p). To make (S, p) not acceptable (S', p') either has to successfully undercut (S, p) or one of (S, p)'s defenders. However, by Property 9, since (S', p')'s corresponding set of agents is less trustworthy than those of (S, p) it is not stronger than (S, p) and so cannot successfully undercut it. Furthermore, since the defenders in (ii) are also stronger than (S, p), (S', p') cannot undercut them either, and so it will fail to make (S, p) not acceptable.  $\Box$ 

This result shows the importance of Property 9 — when it holds, it prevents arguments based on less trustworthy agents from making otherwise acceptable arguments unacceptable, and thus altering what  $Ag_i$  takes as being proven.

Note that the desiderata are not independent:

PROPOSITION 2. Property 2 implies Property 3 and Property 7 implies Property 8.

**PROOF.** P2 requires that given paths from  $Ag_i$  to  $Ag_j$  and  $Ag_k$ , then  $tr(Ag_i, Ag_j) \leq tr(Ag_i, Ag_k)$  if and only if length $(Ag_i, Ag_j)$ is greater than or equal to length $(Ag_i, Ag_k)$ . If this is the case, then given a path  $\langle Ag_i, \ldots Ag_j, \ldots Ag_k \rangle$  it is clear that the path from  $Ag_i$  to  $Ag_k$  is longer than the path to  $Ag_j$  and so  $tr(Ag_i, Ag_k)$ will be less than or equal to  $tr(Ag_i, Ag_j)$ , fulfilling P3.

Similarly, P7 requires that if  $Ag_i$  has two arguments (S, p) and (S', p'), then  $bel_i(p) \leq bel_i(p')$  iff  $|S| \geq |S'|$ . If  $S \supseteq S'$  then this will imply that  $|S| \geq |S'|$  and hence  $bel_i(p) \leq bel_i(p')$ , fulfilling P8.  $\Box$ 

However these pairs of properties are distinct:

PROPOSITION 3. Property 3 does not imply Property 2 and Property 8 does not imply Property 7.

**PROOF.** To prove that the first of each of these properties does not imply the second, it suffices to show a single instance where it is not the case. For P3 and P2 we do this by choosing a specific operator for  $\otimes^{tr}$ . If we use min, then P3 will hold for any assignment of trust values along the path  $\langle Ag_i, \ldots Ag_j, \ldots Ag_k \rangle$ , for example one with minimum value 0.5. However, with the same operator, we can construct a much longer path where the minimum trust value is 0.8, violating Property 2.

The counter-example for the second pair of properties is analogous — combining beliefs with min means a small set of support can easily have a smaller belief value than a large set.  $\Box$ 

## 4. TRUST ARGUMENTATION

Having identified a system of trust argumentation and some desiderata for it, in this section we explore its properties.

#### 4.1 **Properties of the system**

We start by identifying which possible instantiations of the combined trust and argumentation model will satisfy the desiderata in the sense of guaranteeing that the properties will always hold. We begin with Properties 1–3 which depend upon the choice of  $\otimes^{tr}$ . Two such choices, suggested by Richardson *et al.*[23] are minimum and multiplication. We have:

PROPOSITION 4. Combining trust values along a path in a trust network according to (1) with minimum or multiplication will satisfy Properties 1 and 3 but not Property 2.

PROOF. With associative operations like minimum and multiplication, combining trust values along a path in a trust network is exactly the same as combining a set of trust values. If we combine a set of trust values with minimum, then clearly the resulting value will be exactly the minimum of the values and satisfy Property 1. If we combine two sets of values  $S_1$  and  $S_2$  using minimum, and  $S_1 \subseteq S_2$ , then the minimum of  $S_1$  will be no smaller than the minimum of  $S_2$ , and Property 3 holds. It is equally easy to prove Property 2 does not always hold. If we have two sets  $S_1$  and  $S_2$ and  $S_1 \cap S_2 = \emptyset$ , then even if  $S_2$  is much larger than  $S_1$ , its minimum value can be larger than than that of  $S_1 -$  all the values in  $S_2$  could be 0.8 and all those in  $S_1$  could be 0.3.

Combining a set of values that are no larger than 1 with multiplication will give a value that no larger than any of them, satisfying Property 1. Similarly, if we take the result of multiplying the values in  $S_1$  and then multiply by the values in  $S_2 - S_1$  for  $S_1 \subseteq S_2$ , the value we have won't increase, satisfying Property 3. However, with two unconnected sets  $S_1$  and  $S_2$  there is no necessary relationship between the product of the values in the sets and so Property 2 will not always hold.  $\Box$  The issue with satisfying Property 2 is that both minimum and multiplication are applied link by link so there is no way to they can meet a criterion that applies to the whole path. If we stretch the definition of computing trust values along a path to allow trust values to be combined by functions that take the whole path as arguments, then we can easily show that:

PROPOSITION 5. Combining trust values along a path in a trust network in such a way that the trust value is inversely proportional to the length of the path will satisfy Properties 2 and 3 but not Property 1:

**PROOF.** Property 2 requires  $tr(Ag_i, Ag_j) \leq tr(Ag_i, Ag_k)$  iff length $(Ag_i, Ag_j) \geq length(Ag_i, Ag_k)$  which is obviously true for this combination. By Proposition 2, Property 2 implies Property 3, so Property 3 holds as well. The last part of the result is just as easy to show — since the combination depends only on the length of the path, not on the trust values labelling the arcs, there is no reason why the trust along a path should have any particular relationship with those values.  $\Box$ 

The problem with this approach to propagation, and the problem with Property 2, is that it ignores the values of the individual links. As a result it is easy to construct examples which conflict with intuition — a path with very high valued links creates less trust than a marginally shorter path with very low valued links, and any attempt to bring in the values of the links creates situations in which Property 2 can easily be violated.

Now we consider options for  $\oplus^{tr}$ . Richardson *et al.* [23] suggest maximum and Golbeck *et al.* [10] suggest average<sup>3</sup>, while addition seems a suitable dual operation to consider for the options we considered for  $\otimes^{tr}$ — addition is the dual operation to multiplication for probability theory, and some variants of possibility theory use it as a dual for minimum [9]. Considering all three of these operations, we have:

PROPOSITION 6. Combining trust values over multiple paths in a trust network according to (2) with maximum satisfies Properties 4 and 5, combining using addition satisfies Property 4 but does not satisfy Property 5, and combining using average satisfies Property 5 but does not satisfy Property 4.

PROOF. Since Property 4 specifies that the combination must be greater than or equal to the maximum of the values and Property 5 specifies that it must be less than or equal to the maximum, maximum satisfies both (and will be the only operation to). Adding the two values will clearly give something no smaller than the larger, satisfying Property 4 but won't in general satisfy Property 5 (it will only satisfy it when one value is 0). Average will give something no larger than the larger value, satisfying Property 5, but will only satisfy Property 4 when the values are the same.  $\Box$ 

So addition meets our formulation of Jøsang's property, average obeys the property that we introduced, and maximum meets both.

The third set of properties are those for combining beliefs with  $\otimes^{bel}$ . In our combined trust and argumentation system, we are assuming that the belief values of propositions in  $\Delta_i$  are affected by trust values (and we discuss some ways in which this could be achieved below) but to consider the properties, all we assume for now is that there is some distribution of values:

$$m_i: \Delta_i \mapsto [0, 1]$$

from which we can establish a belief value  $bel_i(\cdot)$ , between 1 and 0, for any formula in  $\Delta_i^4$ . These values are then combined to establish beliefs in the conclusions of arguments. Here we consider multiplication and minimum as possible operations for this combination, following the conjunction operations in probability theory and possibility theory respectively [9]. Given Proposition 4 and the origin of Property 1 it is no surprise to find that:

PROPOSITION 7. Combining belief values according to (3) with minimum or multiplication will satisfy Properties 6 and 8 but not Property 7.

**PROOF.** The proof is the same as for Proposition 4.  $\Box$ 

In order to satisfy Property 7 we need to combine beliefs in a way that depends on the size of the set of support, for example:

**PROPOSITION** 8. Consider an argument A = (S, p) where  $S = \{s_1, \ldots, s_n\}$ . Setting  $bel(p) = \frac{1}{|S|}$  will satisfy Properties 7 and 8 but not Property 6.

**PROOF.** The proof is close to that for Proposition 5. The definition of the belief computation means it clearly satisfies Property 7 and by Proposition 2, Property 8 holds as well. The last part of the result is just as easy to show — since the belief in an argument depends only on the size of the support, not on the belief values of formulae in the support, there is no reason why the overall belief should have any particular relationship with the beliefs of the formulae.  $\Box$ 

Thus we have ways of handling trust and belief which will satisfy the various properties we identified, but we have no set of operations that will simultaneously satisfy all the properties.

The final desiderata that we laid down is Property 9, which relates trust values to the conclusions of arguments. To reason about the conditions under which this will hold, we first need to decide how to convert the trust that an agent  $Ag_i$  has in agent  $Ag_j$  into the belief that  $Ag_i$  has in formulae from  $CS_j$ . In order to obtain priorities over an agent's knowledge — which is the role played by beliefs in our argumentation — [16] simply imports trust values as the priorities, and here we propose the same method, defining the function *ttb* from (4) as:

$$ttb(tr(Ag_i, Ag_j)) = tr(Ag_i, Ag_j) \cdot bel\_limit_i$$

where  $bel_limit_i$  is a scaling factor that, given belief and trust values are between 0 and 1 limits the maximum belief that a trust value can map to. There are two obvious ways to set this:

- L1  $bel_limit_i = 1$
- L2  $bel_limit_i = min_i \{bel_i(s_i) | s_i \in \Sigma_i\}$

so that we either scale the trust values compared to the maximum possible value for beliefs, so that information with a trust value of 1 is considered as believable as anything, or we scale beliefs so that everything in  $\Sigma_i$  is at least as believable as anything  $Ag_i$  is told by another agent.

We also need to determine how  $\succ_i^{arg}$  depends on  $\succ_i^{bel}$ , and there are two obvious ways to do this:

 $\begin{array}{l} \text{O1} \ (S,p) \succ_{i}^{arg} (S',p') \text{ iff } (S,p) \succ_{i}^{bel} (S',p') \\ \text{O2} \ (S,p) \succ_{i}^{arg} (S',p') \text{ iff } (S,p) \succ_{i}^{bel} (S',p') \text{ and } Ag \succ_{i}^{tr} Ag' \\ \text{ for all } Ag \text{ corresponding to } S \text{ and } Ag' \text{ corresponding to } S'. \end{array}$ 

<sup>&</sup>lt;sup>3</sup>Average is not usually considered as a binary operation, but it can be expressed in such a form, see, for example [25].

<sup>&</sup>lt;sup>4</sup>The reason for describing the allocation of belief values in this indirect way is that it is required by some approaches to handling uncertainty, including possibility theory [9] which we will make use of below.

With these aspects of the model instantiated, we can consider which combinations of the various features of the model satisfy Property 9. We have:

**PROPOSITION 9.** A trust argumentation system that uses minimum for  $\otimes^{tr}$ , maximum for  $\oplus^{tr}$ , minimum for  $\otimes^{bel}$  and adopts L2 and O1 satisfies Property 9.

PROOF. Property 9 requires the strength of an argument to be determined by the trust  $Ag_i$  has in the corresponding agents so that arguments with less trustworthy corresponding agents are weaker. L2 means that no formulae from any  $CS_j$  can be believed more than one from  $\Sigma_i$ , and using minimum to combine belief values means that the strength of any argument will be determined by the trustworthiness of the corresponding agents (a low belief from  $\Sigma_i$  cannot hide an argument's dependency on an untrustworthy agent).  $\Box$ 

Examining the proof, it is clear why we need to have  $bel_limit_i$ in the model — without it, there is nothing to stop a highly trusted source supplying information that ends up supporting a weak argument by virtue of another piece of the support which comes from  $Ag_i$  itself having a low degree of belief. This, in turn might lead to an argument supported by information from a less trusted source being stronger than an argument based on information from a more trusted source. Exactly this line of reasoning leads us to:

PROPOSITION 10. A trust argumentation system that that uses minimum for  $\otimes^{tr}$ , maximum for  $\oplus^{tr}$ , minimum for  $\otimes^{bel}$  and adopts L1 and O1 does not satisfy Property 9 unless bel(s) = 1 for every  $s \in \Sigma_i$ .

**PROOF.** *Immediate from the proof of Proposition 9.*  $\Box$ 

so not adopting  $L2^5$  doesn't prevent a trust argumentation system meeting our benchmark of performance, Property 9, but means it can only do so under rather restricted circumstances.

Proposition 9 and Proposition 1 tell us that using possibility-style maximum and minimum operations for trust and argumentation — an instantiation of our trust-argumentation system that we will call  $TA_1$  — can guarantee what we have argued is desirable behavior. What about using multiplication, which as we have remarked above, fits more naturally with a probabilistic interpretation of belief? It turns out that:

**PROPOSITION** 11. A trust argumentation system that uses minimum for  $\otimes^{tr}$ , maximum for  $\oplus^{tr}$ , multiplication for  $\otimes^{bel}$  and adopts L2 and O1 does not satisfy Property 9

PROOF. Since the result is only that the system does not satisfy the property, a counter example will suffice. Consider all propositions in  $\Sigma_i$  have belief 1. (S, p) includes just one formula that isn't from  $\Sigma_i$ , it comes from  $CS_j$ , and  $tr(Ag_i, Ag_j) = 0.7$ .  $bel_i(S, p)$ is thus 0.7. (S', p') includes just two formulae that aren't from  $\Sigma_i$ . These formulae come from  $CS_k$  and  $CS_l$ , and  $tr(Ag_i, Ag_k) =$  $tr(Ag_i, Ag_l) = 0.8$ . Thus  $bel_i(p') = 0.64$  and the argument is not as strong as the argument which depends on information from a less-trusted source.  $\Box$ 

As the proof shows, the reason that this second trust argumentation system fails to satisfy Property 9 is because multiplying belief values will generate arguments with low beliefs and with O1 determining the order over arguments, this means weak arguments can be generated using information from highly trusted agents. One way to prevent this is to use O2 to determine the order over arguments. We have: **PROPOSITION** 12. A trust argumentation system that uses minimum for  $\otimes^{tr}$ , maximum for  $\oplus^{tr}$ , multiplication for  $\otimes^{bel}$  and adopts L2 and O2 satisfies Property 9.

**PROOF.** Immediate from the definition of 02.  $\Box$ 

The disadvantage of adopting O2 is that it will only produce a partial order for  $\succ_i^{arg}$ , and given the role  $\succ_i^{arg}$  plays in defining the acceptability, this will affect the reasoning the agents can carry out.

#### 4.2 Trust thresholds

Let's look at one way we can use  $TA_1$ . Consider that  $Ag_i$  has a *trust threshold* of  $\alpha$ , a trust value for agents below which it wishes not to use information from them. If we give arguments whose status is unaffected by information from agents whose trust value is below the threshold  $\alpha$  the name  $\alpha$ -safe then:

**PROPOSITION 13.** If  $Ag_i$  has a  $TA_1$  argumentation system:

 $\langle Ags, \mathcal{A}(\Delta_i), Undercut, \succ_i^{arg}, \mathcal{T} \rangle$ 

where all formulae in  $\Sigma_i$  have belief value 1, and  $Ag_i$  has a trust threshold  $\alpha$ , then all arguments with a level of belief above  $\alpha$  are  $\alpha$ -safe.

**PROOF.** Setting the belief of all formulae in  $\Sigma_i$  to 1 ensures that the belief values of arguments directly reflect their trust values making the belief value equal to the threshold easy to establish<sup>6</sup>. If an argument A is acceptable, and has a belief value above  $\alpha$ , then as we recall from the proof of Proposition 1 — any undercutters that aren't weaker than A (and so may be below the trust threshold but not affecting the status of A) must, since A is acceptable, be successfully undercut by stronger arguments. Because of the way that trust is converted into belief and belief values are combined with minimum, none of these arguments can be based on information that comes from an agent trusted less than  $\alpha$ . So not only A, but all of the arguments that determine its status, must be  $\alpha$ -safe.

If an argument A' is not acceptable and it is above the trust threshold, but was successfully defeated, then that defeat must have been by an argument that is above the trust threshold which (since that defeater is successful) means that in the same way as A, this defeater is  $\alpha$ -safe, and hence so is A'.  $\Box$ 

This result is helpful because it shows us that for  $TA_1$  information from agents below the trust threshold has limited impact — it won't change the acceptability or otherwise of arguments above the threshold.

# 5. CONCLUSION

In this paper we presented a formal model that provides a simple combination of argumentation and trust. We examined some of the properties of different instantiations of the model, and showed that the system we called  $TA_1$  has the ability to ensure that arguments grounded in information from untrustworthy agents cannot overrule arguments grounded by more trustworthy agents and under certain conditions can deal with trust thresholds.

This work is distinct from, and complementary to, other existing work on trust and argumentation. The work of Matt *et al.* [18] for example looks at constructing arguments *for* trusting other agents — it is a way to compute the tr values that we assume. In contrast, here we are concerned with computing arguments *with* trust. Similar remarks hold for [20] which looks to construct arguments about the trust that one agent has in another.

<sup>&</sup>lt;sup>5</sup>Or, of course, some other mechanism for preventing the kind of interaction between belief and trust sketched in the proof of Proposition 9.

<sup>&</sup>lt;sup>6</sup>The proof can be altered to deal with formulae in  $\Sigma_i$  having smaller belief values, it would mean replacing the trust threshold in the proof with  $\alpha.min_j \{bel_i(s_j) | s_j \in \Sigma_i\}$ 

Though the system we define is simple, there is more to say about it. Our future work will address aspects of the system that we have not had space to discuss here. We are working on a more extensive analysis of operators for the trust argumentation systems, as well as expanding the notion of trust threshold to what we call the *trust budget* — if an agent is prepared to tolerate a certain overall amount of distrust in all the information it uses in all of its arguments, how does this affect what it finds acceptable? Other topics of interest are combining what we have here with the use of argumentation to establish trust values, and the use of more complex methods of representing trust than the simple numerical approach we adopt here.

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