

# Resource Logics with a Diminishing Resource

## Extended Abstract

Natasha Alechina  
University of Nottingham  
Nottingham, UK  
nza@cs.nott.ac.uk

Brian Logan  
University of Nottingham  
Nottingham, UK  
bsl@cs.nott.ac.uk

### ABSTRACT

Model-checking resource logics with production and consumption of resources is a computationally hard and often undecidable problem. We show that it is more feasible under the assumption that there is at least one *diminishing resource*, that is, a resource which is consumed by every action.

### KEYWORDS

Model-checking; resources

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## 1 INTRODUCTION

There has been a considerable amount of work on resource logics interpreted over structures where agents' actions produce and consume resources, for example [2, 3, 6–9, 12–14, 17–19]. There exists also a large body of related work on reachability and non-termination problems in energy games and games on vector addition systems with state [1, 11, 15, 16, 21]. The resource logics considered in this paper are extensions of the Alternating Time Temporal Logic (ATL), [10]. For ATL under imperfect information and with perfect recall uniform strategies,  $ATL_{iR}$ , the model-checking problem is undecidable for three or more agents [20]. It is however decidable in the case of bounded strategies [23].

In this paper we introduce a special kind of models for resource logics satisfying a restriction that one of the resources is always consumed by each action. This is a very natural setting that occurs in many verification problems. One obvious example of such a resource is time. Other examples include systems where agents have a non-rechargeable battery and where all actions consume energy, e.g., nodes in a wireless sensor network; and systems where agents have a store of propellant that cannot be replenished during the course of a mission and all actions of interest involve manoeuvring, e.g., a constellation of satellites. We call this special resource that is consumed by all actions a *diminishing resource*.

We study  $RB \pm ATL^\#$  and  $RB \pm ATL_{iR}^\#$ , diminishing resource versions of Resource-Bounded Alternating Time Temporal Logic ( $RB \pm ATL$ ) [5]. The model-checking problem for  $RB \pm ATL$  is known to be 2EXPTIME-complete [6], while  $RB \pm ATL^\#$  model-checking is in PSPACE if resource bounds are written in unary. In the case of

$RB \pm ATL_{iR}^\#$ , the result of [23] does not apply immediately because the bound is not fixed in advance, but its model checking problem is decidable in EXPSpace given encoding in unary. We also study  $RAL^\#$ , a diminishing resource version of Resource Agent Logic (RAL) [13]. Decidability of  $RAL^\#$  follows from the result on the decidability of RAL on bounded models [13], but the PSPACE upper bound (for unary encoding) is new.

## 2 $RB \pm ATL^\#$

The syntax of  $RB \pm ATL^\#$  is defined relative to the following sets:  $Agt = \{a_1, \dots, a_n\}$  is a set of  $n$  agents,  $Res = \{res_1, \dots, res_r\}$  is a set of  $r$  resource types,  $\Pi$  is a set of propositions, and  $\mathcal{B} = \mathbb{N}^{Res \times Agt}$  is a set of resource bounds (resource allocations to agents). Elements of  $\mathcal{B}$  are vectors of length  $n$  where each element is a vector of length  $r$ . We will denote by  $\mathcal{B}_A$  (for  $A \subseteq Agt$ ) the set of possible resource allocations to agents in  $A$ . Formulas of  $RB \pm ATL^\#$  are defined by:

$$\phi, \psi ::= p \mid \neg\phi \mid \phi \vee \psi \mid \langle\langle A^b \rangle\rangle \circ \phi \mid \langle\langle A^b \rangle\rangle \phi \mathcal{U} \psi \mid \langle\langle A^b \rangle\rangle \phi \mathcal{R} \psi$$

where  $p \in \Pi$ ,  $A \subseteq Agt$ , and  $b \in \mathcal{B}_A$ .  $\langle\langle A^b \rangle\rangle \circ \phi$  means that a coalition  $A$  can ensure that the next state satisfies  $\phi$  under resource bound  $b$ .  $\langle\langle A^b \rangle\rangle \phi \mathcal{U} \psi$  means that  $A$  has a strategy to enforce  $\psi$  while maintaining the truth of  $\phi$ , and the cost of this strategy is at most  $b$ .  $\langle\langle A^b \rangle\rangle \phi \mathcal{R} \psi$  means that  $A$  has a strategy to maintain  $\psi$  until and including the time when  $\phi$  becomes true, or to maintain  $\psi$  forever if  $\phi$  never becomes true, and the cost of this strategy is at most  $b$ . The language is interpreted on the following structures:

*Definition 2.1.* A resource-bounded concurrent game structure with diminishing resource (RB-CGS<sup>#</sup>) is a tuple  $M = (Agt, Res, S, \Pi, \pi, Act, d, c, \delta)$  where:

- $Agt, Res$  and  $\Pi$  are as above; the first resource type in  $Res$  is the distinguished diminishing resource;
- $S$  is a non-empty finite set of states;
- $\pi : \Pi \rightarrow \wp(S)$  is a truth assignment that associates each  $p \in \Pi$  with a subset of states where it is true;
- $Act$  is a non-empty set of actions;
- $d : S \times Agt \rightarrow \wp(Act) \setminus \{\emptyset\}$  is a function that assigns to each  $s \in S$  a non-empty set of actions available to each agent  $a \in Agt$ .
- $c : S \times Act \rightarrow \mathbb{Z}^r$  is a partial function that maps a state  $s$  and an action  $\sigma$  to a vector of integers, where a positive (negative) integer in position  $i$  indicates consumption (production) of resource  $r_i$  by the action. The first position in the vector is always at most  $-1$ .
- $\delta : S \times Act^{|Agt|} \rightarrow S$  is a partial function that maps every  $s \in S$  and  $\sigma \in d(s, a_1) \times \dots \times d(s, a_n)$  to a state resulting from executing  $\sigma$  in  $s$ .

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In what follows, we use the usual point-wise notation for vector comparison and addition, and, given a function  $f$  returning a vector, we denote by  $f_i$  the function that returns the  $i$ -th component of the vector returned by  $f$ . Given an RB-CGS<sup>#</sup>  $M$  and a state  $s \in S$ , a *joint action by a coalition*  $A \subseteq \text{Agt}$  is a tuple  $\sigma = (\sigma_a)_{a \in A}$  such that  $\sigma_a \in d(s, a)$ . The set of all joint actions for  $A$  at state  $s$  is denoted by  $D_A(s)$ . Given a joint action by  $\text{Agt}$ ,  $\sigma \in D_{\text{Agt}}(s)$ ,  $\sigma_A$  denotes the joint action executed by  $A$  as part of  $\sigma$ :  $\sigma_A = (\sigma_a)_{a \in A}$ . The set of all possible outcomes of a joint action  $\sigma \in D_A(s)$  at state  $s$  is:  $\text{out}(s, \sigma) = \{s' \in S \mid \exists \sigma' \in D_{\text{Agt}}(s) : \sigma = \sigma'_A \wedge s' = \delta(s, \sigma')\}$ . A *strategy for a coalition*  $A \subseteq \text{Agt}$  in an RB-CGS<sup>#</sup>  $M$  is a mapping  $F_A : S^+ \rightarrow \text{Act}^{|A|}$  such that, for every  $\lambda \in S^+$ ,  $F_A(\lambda) \in D_A(\lambda[|\lambda|])$ . A computation  $\lambda$  is consistent with a strategy  $F_A$  iff, for all  $i$ ,  $1 \leq i < |\lambda|$ ,  $\lambda[i+1] \in \text{out}(\lambda[i], F_A(\lambda[1, i]))$ . We denote by  $\text{out}(s, F_A)$  the set of all computations  $\lambda$  starting from  $s$  that are consistent with  $F_A$ . Given a bound  $b \in \mathcal{B}$ , a computation  $\lambda \in \text{out}(s, F_A)$  is  $b$ -consistent with  $F_A$  iff, for every  $i \geq 0$ , for every  $a \in A$ ,  $b_a - \sum_{j=0}^{i-1} c(F_a(\lambda[0, j])) \geq c(F_a(\lambda[0, i]))$ .

A computation  $\lambda$  is  $b$ -maximal for a strategy  $F_A$  if it cannot be extended further while remaining  $b$ -consistent. The set of all maximal computations starting from state  $s$  that are  $b$ -consistent with  $F_A$  is denoted by  $\text{out}(s, F_A, b)$ .

Given an RB-CGS<sup>#</sup>  $M$  and a state  $s$  of  $M$ , the truth of an RB $\pm$ ATL<sup>#</sup> formula  $\phi$  with respect to  $M$  and  $s$  is defined as follows (omitting the cases for propositions,  $\neg$  and  $\wedge$ ):

- $M, s \models \langle\langle A^b \rangle\rangle \phi$  iff  $\exists$  strategy  $F_A$  such that for all  $b$ -maximal  $\lambda \in \text{out}(s, F_A, b)$ :  $|\lambda| \geq 2$  and  $M, \lambda[2] \models \phi$ ;
- $M, s \models \langle\langle A^b \rangle\rangle \phi \mathcal{U} \psi$  iff  $\exists$  strategy  $F_A$  such that for all  $b$ -maximal  $\lambda \in \text{out}(s, F_A, b)$ ,  $\exists i$  such that  $1 \leq i \leq |\lambda|$ :  $M, \lambda[i] \models \psi$  and  $M, \lambda[j] \models \phi$  for all  $j \in \{1, \dots, i-1\}$ ;
- $M, s \models \langle\langle A^b \rangle\rangle \phi \mathcal{R} \psi$  iff  $\exists$  strategy  $F_A$  such that for all  $b$ -maximal  $\lambda \in \text{out}(s, F_A, b)$ , either  $\exists i$  such that  $1 \leq i \leq |\lambda|$ :  $M, \lambda[i] \models \phi$  and  $M, \lambda[j] \models \psi$  for all  $j \in \{1, \dots, i\}$ ; or,  $M, \lambda[j] \models \psi$  for all  $j$  such that  $1 \leq j \leq |\lambda|$ .

The following theorem is proved by demonstrating a model-checking algorithm for RB  $\pm$  ATL<sup>#</sup>, see [4]:

**THEOREM 2.2.** *The model-checking problem for RB  $\pm$  ATL<sup>#</sup> is decidable in PSPACE (under unary encoding).*

### 3 RB $\pm$ ATL<sup>#</sup><sub>iR</sub>

In this section, we study RB  $\pm$  ATL<sup>#</sup><sub>iR</sub>, RB  $\pm$  ATL<sup>#</sup> with imperfect information and perfect recall. To model imperfect information, RB-CGS<sup>#</sup> are extended with an indistinguishability relation  $\sim_a$  on states, for every agent  $a$ . This relation can be lifted to finite sequences of states. Strategies under imperfect information should be *uniform*: if agent  $a$  is uncertain whether the history so far is  $\lambda$  or  $\lambda'$  ( $\lambda \sim_a \lambda'$ ), then the strategy for  $a$  should return the same action for both  $\lambda$  and  $\lambda'$ :  $F_a(\lambda) = F_a(\lambda')$ . A strategy  $F_A$  for a group of agents  $A$  is uniform if it is uniform for every agent in  $A$ . In what follows, we consider *strongly uniform* strategies [22], that require the existence of a uniform strategy from all indistinguishable states:

- $M, s \models \langle\langle A^b \rangle\rangle \phi$  under strong uniformity iff there exists a uniform strategy,  $F_A$ , such that, for all  $s' \sim_a s$  where  $a \in A$ , for all  $\lambda \in \text{out}(s', F_A, b)$ ,  $|\lambda| > 1$  and  $M, \lambda[2] \models \phi$ .

The truth definitions for  $\langle\langle A^b \rangle\rangle \phi \mathcal{U} \psi$  and  $\langle\langle A^b \rangle\rangle \phi \mathcal{R} \psi$  are also modified to require the existence of a *uniform* strategy from all states  $s'$  indistinguishable from  $s$  by any  $a \in A$ .

**THEOREM 3.1.** *The model-checking problem for RB  $\pm$  ATL<sup>#</sup><sub>iR</sub> is decidable in EXPSpace (under unary encoding).*

### 4 RAL<sup>#</sup>

RAL<sup>#</sup> is obtained by modifying the definition of RAL [13] for the diminishing resource setting. The sets  $\text{Agt}$ ,  $\text{Res}$ , and  $\Pi$  are as before. An *endowment (function)*  $\eta : \text{Agt} \times \text{Res} \rightarrow \mathbb{N}$  assigns resources to agents:  $\eta_a(r) = \eta(a, r)$  is the amount of resource agent  $a$  has of resource type  $r$ .  $\text{En}$  denotes the set of all possible endowments. Formulas of RAL<sup>#</sup> are defined by:

$$\phi, \psi ::= p \mid \neg \phi \mid \phi \wedge \phi \mid \langle\langle A \rangle\rangle_B^{\downarrow} \phi \mid \langle\langle A \rangle\rangle_B^{\uparrow} \phi \mid \langle\langle A \rangle\rangle_B^{\downarrow} \phi \mathcal{U} \psi \mid \langle\langle A \rangle\rangle_B^{\uparrow} \phi \mathcal{U} \psi \mid \langle\langle A \rangle\rangle_B^{\downarrow} \phi \mathcal{R} \psi \mid \langle\langle A \rangle\rangle_B^{\uparrow} \phi \mathcal{R} \psi$$

where  $p \in \Pi$ ,  $A, B \subseteq \text{Agt}$ , and  $\eta \in \text{En}$ . Unlike in RB  $\pm$  ATL<sup>#</sup>, in RAL<sup>#</sup> there are two types of cooperation modalities,  $\langle\langle A \rangle\rangle_B^{\downarrow}$  and  $\langle\langle A \rangle\rangle_B^{\uparrow}$ . In both cases, the actions performed by agents in  $A \cup B$  consume and produce resources (actions by agents in  $\text{Agt} \setminus (A \cup B)$  do not change their resource endowment). The meaning of  $\langle\langle A \rangle\rangle_B^{\uparrow} \phi$  is otherwise the same as in RB  $\pm$  ATL<sup>#</sup>. The formula  $\langle\langle A \rangle\rangle_B^{\downarrow} \phi$  requires that the strategy uses the resources *currently* available to the agents.

The models of RAL<sup>#</sup> are RB-CGS<sup>#</sup>. Strategies are also defined as for RB  $\pm$  ATL<sup>#</sup>. However, to evaluate formulas with a down arrow, such as  $\langle\langle A \rangle\rangle_B^{\downarrow} \phi$ , we need the notion of *resource-extended computations*. A *resource-extended* computation  $\lambda \in (S \times \text{En})^+$  is a sequence over  $S \times \text{En}$  such that the restriction to states (the first component), denoted by  $\lambda|_S$ , is a path in the underlying model. The projection of  $\lambda$  to the second component is denoted by  $\lambda|_{\text{En}}$ . A  $(\eta, s_A, B)$ -*computation*,  $\lambda$ , is a resource-extended computation iff for all  $i = 1, \dots$  with  $\lambda[i] := (s_i, \eta^i)$  there is an action profile  $\sigma \in d(\lambda|_S[i])$  such that:

- $\eta^0 = \eta$  ( $\eta$  describes the initial resource distribution);
- $F_A(\lambda|_S[1, i]) = \sigma_A$  ( $A$  follow their strategy);
- $\lambda|_S[i+1] = \delta(\lambda|_S[i], \sigma)$  (transition according to  $\sigma$ );
- for all  $a \in A \cup B$ :  $\eta_a^i \geq c(\lambda|_S[i], \sigma_a)$  (each agent has enough resources to perform its action);
- for all  $a \in A \cup B$ :  $\eta_a^{i+1} = \eta_a^i - c(\lambda|_S[i], \sigma_a)$  (resources are updated);
- for all  $a \in \text{Agt} \setminus (A \cup B)$  and  $r \in \text{Res}$ :  $\eta_a^{i+1}(r) = \eta_a^i(r)$  (the resources of agents not in  $A \cup B$  do not change).

$\text{out}(s, \eta, F_A, B)$  is the set of all  $(\eta, F_A, B)$ -computations starting in  $s$ . The truth definition is given with respect to a model, a state, and an endowment  $\eta$ :

- $M, s, \eta \models \langle\langle A \rangle\rangle_B^{\downarrow} \phi$  iff there is a strategy  $F_A$  for  $A$  such that for all  $\lambda \in \text{out}(s, \eta, F_A, B)$ ,  $|\lambda| > 1$  and  $M, \lambda|_S[2], \lambda|_{\text{En}}[2] \models \phi$

and similarly for  $\langle\langle A \rangle\rangle_B^{\uparrow} \phi \mathcal{U} \psi$  and  $\langle\langle A \rangle\rangle_B^{\downarrow} \phi \mathcal{R} \psi$ . The cases for  $\langle\langle A \rangle\rangle_B^{\downarrow} \phi$ ,  $\langle\langle A \rangle\rangle_B^{\uparrow} \phi \mathcal{U} \psi$ ,  $\langle\langle A \rangle\rangle_B^{\downarrow} \phi \mathcal{R} \psi$  quantify over  $\lambda \in \text{out}(s, \zeta, F_A, B)$ .

**THEOREM 4.1.** *The model-checking problem for RAL<sup>#</sup> is decidable in PSPACE (under unary encoding).*

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